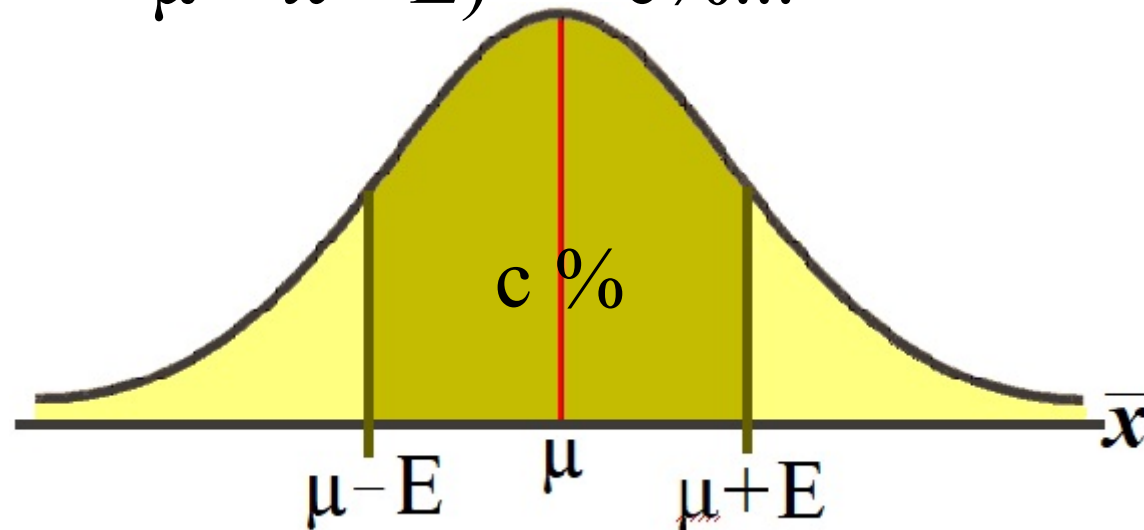


- I. For a population, its mean “ $\mu$ ” is approximated by “ $\bar{x}$ ” (*i.e.*, the mean of a random sample).
- II. The “margin of error,” is  $E = |\bar{x} - \mu|$ ; *i.e.*, how far “ $\bar{x}$ ” is from the true (population) mean “ $\mu$ ”
- III. The “confidence interval” for  $\bar{x}$  in a distribution of sample means is given by  $\bar{x} - E < \mu < \bar{x} + E$ . The confidence level is expressed by a percent,  $P(\bar{x} - E < \mu < \bar{x} + E) = c\%$ ...



## IV. Using the standard normal distribution:

and  $z = (\bar{x} - \mu_{\bar{x}}) \div \sigma_{\bar{x}}$   
 find the  $z$ -score, “ $z_c$ ” such that...

$$P(-z_c < z < z_c) \approx c\%$$

“E” can be determined as follows,

*solve*  $z_c = (\mu + E - \mu_{\bar{x}}) \div \sigma_{\bar{x}}$

multiply by “ $\sigma_{\bar{x}}$ ”, to obtain


$$z_c \times \sigma_{\bar{x}} = \mu + E - \mu_{\bar{x}}$$

then use  $\sigma_{\bar{x}} = \sigma \div \sqrt{n}$  &  $\mu_{\bar{x}} = \mu$

to get  $z_c \times \sigma \div \sqrt{n} = \mu + E - \mu$

**VOILA!**

$$z_c \times \sigma \div \sqrt{n} = E$$

 p.363

“ $z_c$ ” is referred to as the “critical value”

V. The confidence interval/level & margin of error model is statistically valid provided:

(1) the original/raw “ $\mathbf{x}$ ” data is a normal distribution  
**OR**

(2) the original/raw “ $\mathbf{x}$ ” data set’s distribution is not significantly skewed (*i.e.*, its graph is basically bell-shaped), and that the sampling “ $\overline{\mathbf{x}}$ ” data is a random sample whose size is  $n \geq 30$

VI. Examples (pp.370-372): #12,14a,18,22

HW: pp.369-373 / #1,3,5,11,13a,15a&d,19,21,23

Read pp.374-381 (section 7.2)